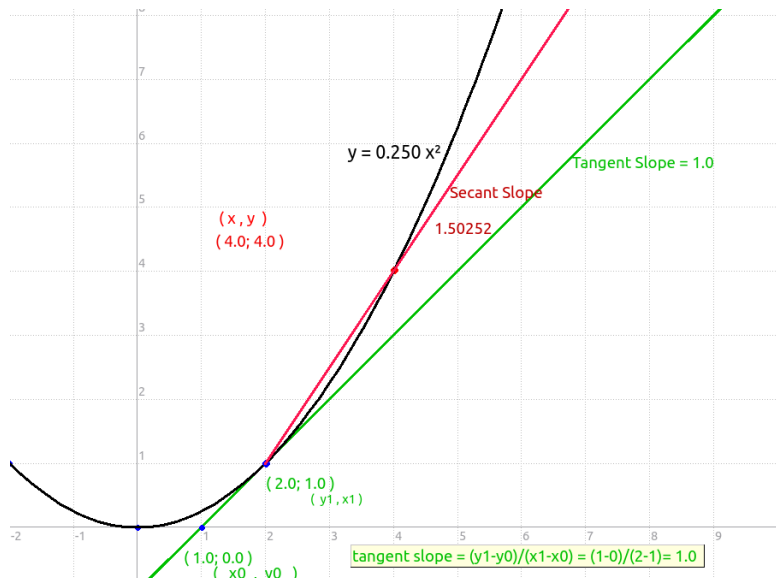


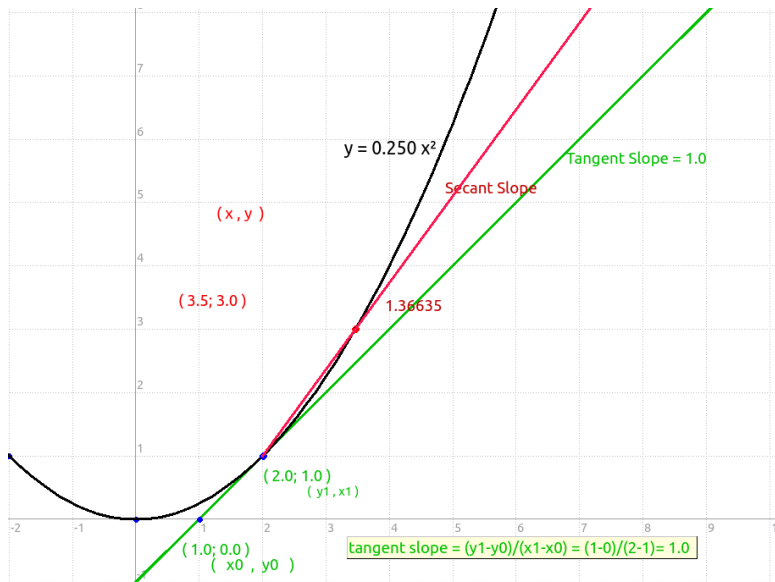
# Right Hand Limit

$x \rightarrow 2^+$	4.0		
Secant Slope	1.5		



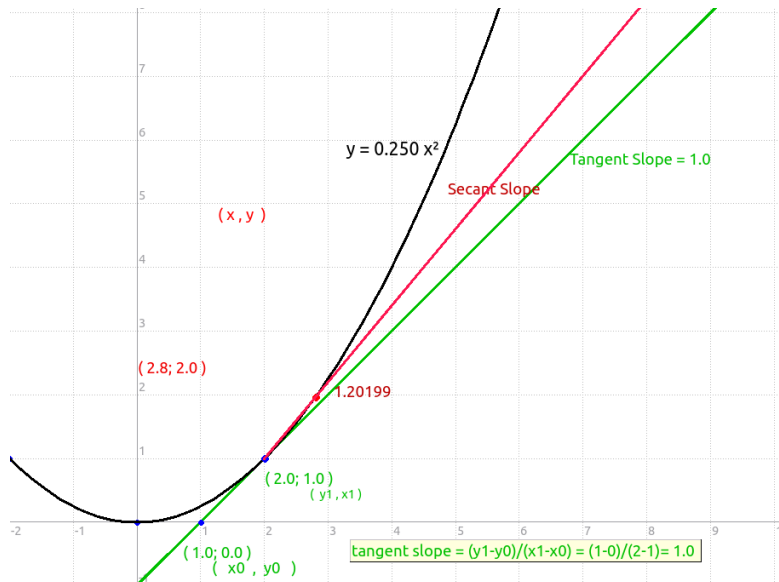
# Right Hand Limit

$x \rightarrow 2^+$	4.0	3.5	
Secant Slope	1.5	1.4	



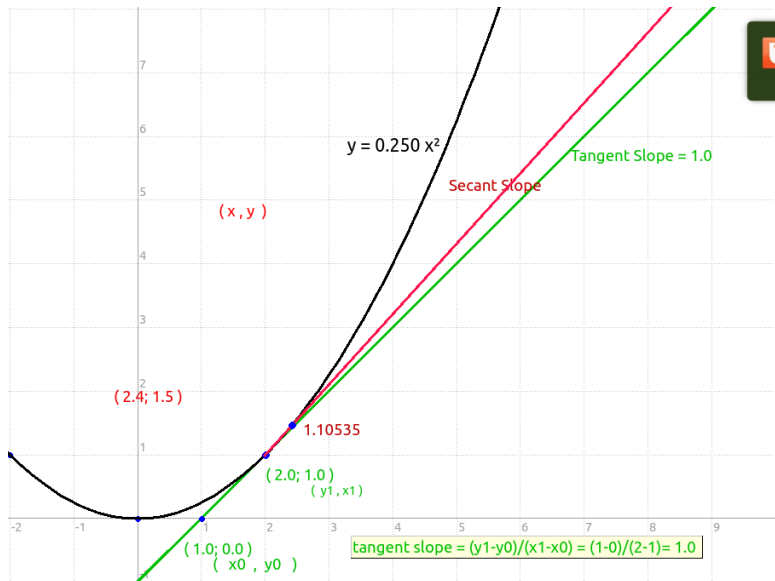
# Right Hand Limit

$x \rightarrow 2^+$	4.0	3.5	2.8
Secant Slope	1.5	1.4	1.2



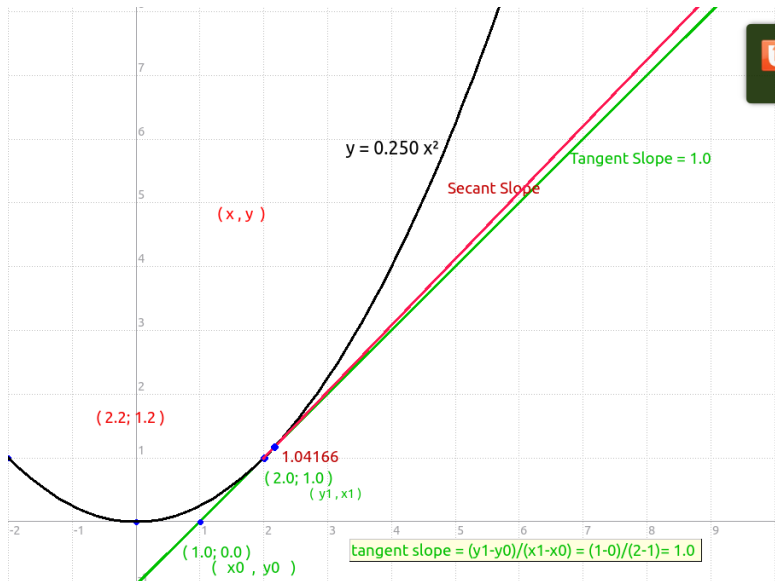
## Right Hand Limit

$x \rightarrow 2^+$	4.0	3.5	2.8	2.4
Secant Slope	1.5	1.4	1.2	1.1



## Right Hand Limit

$x \rightarrow 2^+$	4.0	3.5	2.8	2.4	2.2
Secant Slope	1.5	1.4	1.2	1.1	1.04



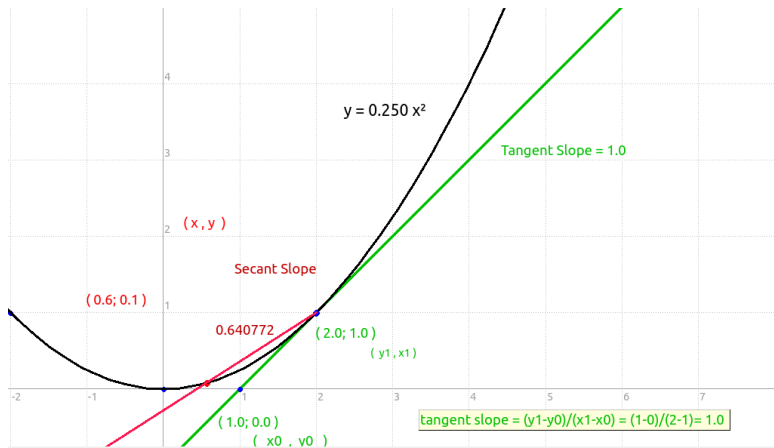
## Right Hand Limit

$$y = f(x) = \frac{1}{4}x^2$$

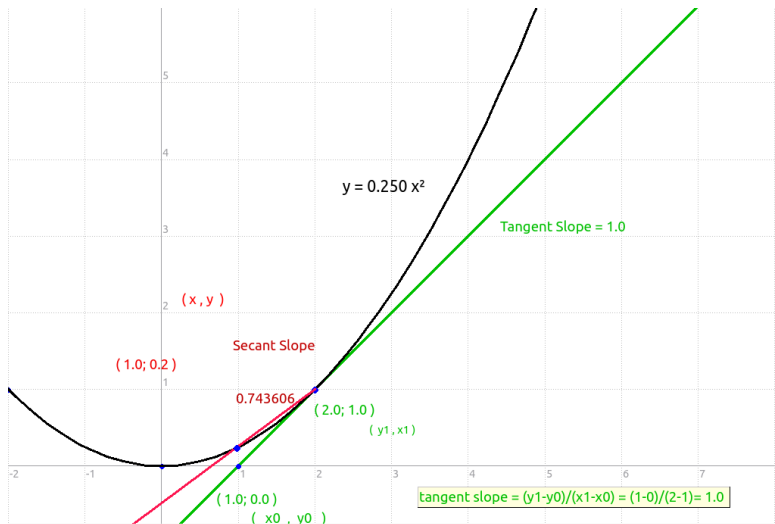
$x \rightarrow 2^+$	4.0	3.5	2.8	2.4	2.2	$\rightarrow 2^+$ (from right)
Secant Slope	1.5	1.4	1.2	1.1	1.04	$\rightarrow 1.0^+$ (Tangent Slope)

$$\text{Tangent Slope} = \lim_{x \rightarrow 2^+} [\text{Secant Slope}] = 1.0$$

# Left Hand Limit

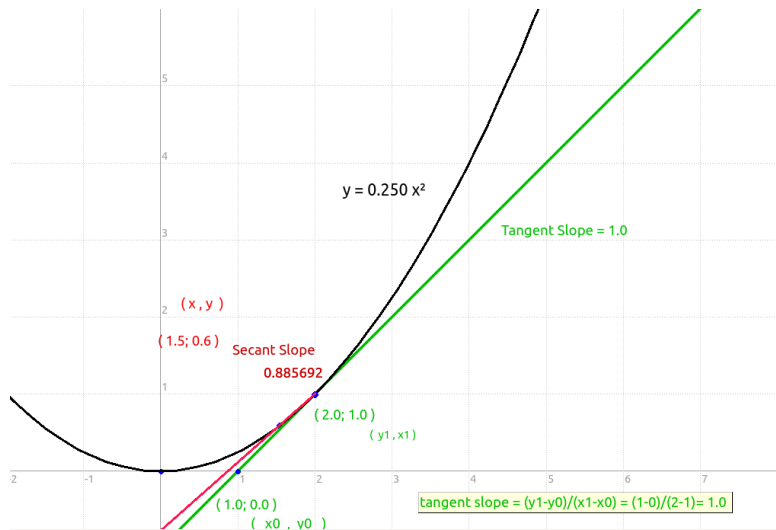


# Left Hand Limit

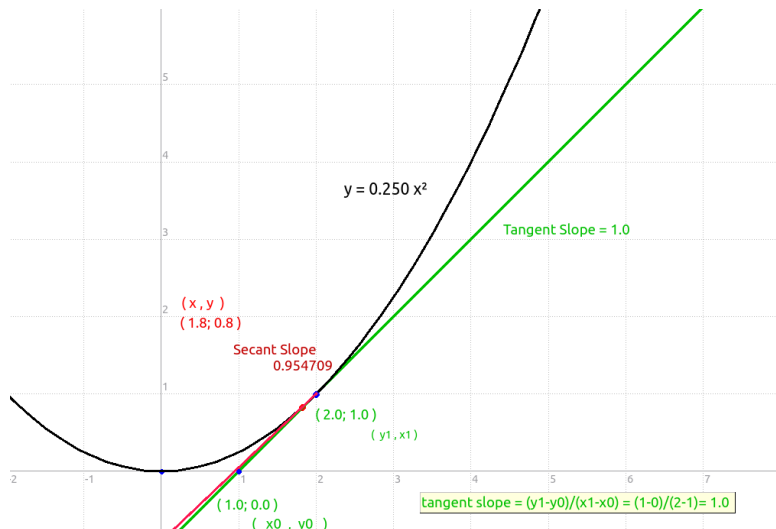




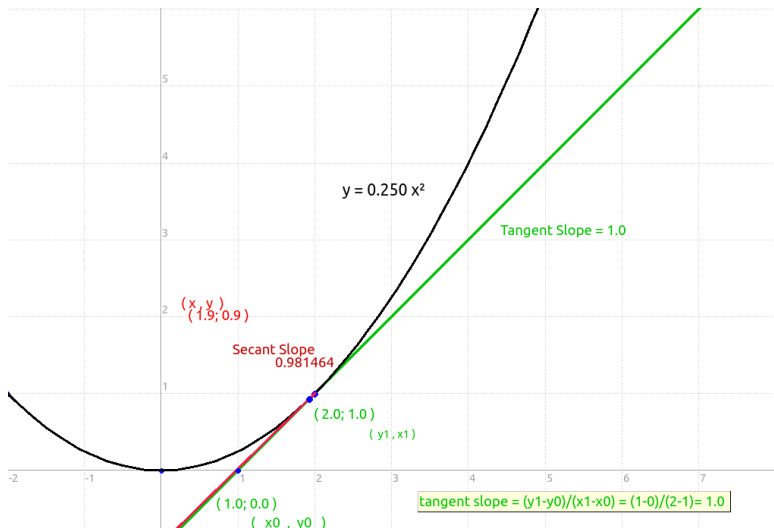
# Left Hand Limit



# Left Hand Limit



# Left Hand Limit



## Left Hand Limit

$$y = f(x) = \frac{1}{4}x^2$$

$x \rightarrow 2^-$	0.6	1.0	1.5	1.8	1.9	$\rightarrow 2^-$ (from left)
Secant Slope	0.6	0.7	0.88	0.95	0.98	$\rightarrow 1.0^-$ (Tangent Slope)

$$\text{Tangent Slope} = \lim_{x \rightarrow 2^-} [\text{Secant Slope}] = 1.0$$

# LHL = RHL $\Rightarrow$ Limit

▶  $y = f(x) = \frac{1}{4}x^2$

▶

$x \rightarrow 2^-$	0.6	1.0	1.5	1.8	1.9	$\rightarrow 2^-$
Secant Slope	0.6	0.7	0.88	0.95	0.98	$\rightarrow 1.0^-$

▶ Tangent Slope =  $\lim_{x \rightarrow 2^-}$  [ Secant Slope ] = 1.0

▶

$x \rightarrow 2^+$	4.0	3.5	2.8	2.4	2.2	$\rightarrow 2^+$
Secant Slope	1.5	1.4	1.2	1.1	1.04	$\rightarrow 1.0^+$

▶ Tangent Slope =  $\lim_{x \rightarrow 2^+}$  [ Secant Slope ] = 1.0

▶ LHL  $_{x \rightarrow 2} =$  RHL  $_{x \rightarrow 2} = 1.0 \Rightarrow$

The Limit exists and is equal to 1.0

▶  $\lim_{x \rightarrow 2}$  [Slope of Secant Line] = Slope of Tangent Line = 1.0.