## Combinatorics Seminar

Injective labelings of graphs
Jacques Verstraete (UC San Diego)

Abstract: Abstract: In this talk I will discuss the problem of coloring the vertices of a graph with k colors such that the neighborhood $N(v)$ contains all $k$ colors for every vertex $v$ in the graph. The problem is to maximize the value of $k$ for which such a coloring is possible. We show that if $G$ is a d-regular graph, then the maximum is $k=(1+o(1)) d / l o g d$ and that almost every d-regular graph required at least $(1+o(1)) d / l o g d$ colors. This problem has connections to coding theory, and with this in mind we discuss colorings of the q -ary Hamming cube graphs of dimension n . Some open problems will be given.

Joint work with Bob Chen, Jeong Han Kim and Mike Tait

