Homotopy Algebras Seminar

Additivity and Formality for E_n operads

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Abstract: Let E_n be the little disks operad. It is well known that for n>1, the rational homology of E_n is P_n, the (n-1) shifted Poisson operad. More generally, for all n, E_n has a filtration whose associated graded operad is P_n. Dunn's additivity theorem states that the Boardman-Vogt tensor product of E_k and E_l is E_{k+l}. We will show that this equivalence is compatible with the filtration and, time permitting, explain the generalization of this statement to factorization algebras.

This fact has a number of remarkable consequences. An immediate corollary is the formality theorem for n>2 by induction starting with formality for E_2. Furthermore, the factorization algebra version of the result provides a local-to-global version of the BV-AKSZ formalism in quantum field theory, and sheds new light on the problem of quantization.

Friday, April 24 at 1:00 PM in SEO 1227