Mathematics, Statistics, and Computer Science **@ UIC** 

## **Combinatorics Seminar**

## Degree versions of the Erdos-Ko-Rado and Hilton-Milner theorems

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**Abstract:** A family of sets is intersecting if any two members have a nonempty intersection. We call an intersecting family trivial if all of its members have a nonempty intersection. Let X be a set of n elements. The celebrated Erdos-Ko-Rado theorem (EKR) says that whenever  $n \ge 2k$ , the maximum size of an intersecting family of k-subsets of X is attained by trivial intersecting families. The Hilton-Milner theorem says that the maximum size of a nontrivial intersecting family of k-subsets of X is attained by the family HM, which consists a fixed k-set S and all k-subsets of X that contains a fixed element x\in X-S and at least one element from S. We prove a minimum degree version of the EKR, which implies the EKR as a corollary. We also prove a degree version of the Hilton-Milner theorem for  $n > 30k^2$ .

These are joint works with Jie Han and Hao Huang.

Monday, March 13 at 2:00 PM in SEO 612