

- (9 points) Let  $f(x) = x^3 + 3x^2$ . Find all points that satisfy the conclusion of the Mean Value Theorem on the interval  $[-5, 1]$ .
- (1 point) Sketch a rectangular solid with length  $l$ , width  $w$ , and height  $h$ , all in feet. Write the formulas for volume and surface area of the solid, and make sure to include the units/dimension, e.g. square feet or cubic feet.

(1) MVT says there is at least one point  $x$  in  $(-5, 1)$  where  $f'(x) = \frac{f(1) - f(-5)}{1 - (-5)}$ .

$$f'(x) = 3x^2 + 6x$$

$$\frac{f(1) - f(-5)}{6} = \frac{1 + 3 - (-125 + 75)}{6}$$

$$= \frac{4 - (-50)}{6} = \frac{54}{6} = 9$$

Set  $3x^2 + 6x = 9$

$$3x^2 + 6x - 9 = 0$$

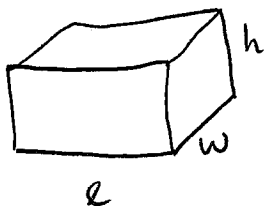
$$3(x + 2x - 3) = 0$$

$$3(x - 1)(x + 3) = 0 \Rightarrow x = 1, -3$$

Note  $x = 1$  is not in the open interval  $(-5, 1)$

So our answer is the pt  $x = 1$ .

(2)



$$\text{Vol} = l \cdot w \cdot h \text{ ft}^3$$

$$\text{SA} = 2lh + 2lw + 2wh \text{ ft}^2$$