## Math 215. Homework 2

due 01/30/08

1. Considering possible remainders of an integer $n$ divided by 3 show that $n^{3}-n$ is divisible by 3 .
2. Show that $|x| \cdot|y|=|x \cdot y|$
3. Show that for $x \geq 0, y \geq 0$ one has

$$
\frac{x+y}{2} \geq \sqrt{x y}
$$

4. Show that for $x>0, y>0$ one has:

$$
\frac{2}{\frac{1}{x}+\frac{1}{y}} \leq \sqrt{x \cdot y}
$$

(i.e. harmonic mean does not exceed geometric mean).

Hint: use "proof backward" method in the last two problems.

