

Name (print) \_\_\_\_\_ Tu/Th Discussion (circle) 12 1 2

\*\*\*\*\* If you use a calculator it must be your own. You must show your work. \*\*\*\*\*

1. (12 points) Suppose that  $\tan t = -\frac{5}{12}$  and  $\cos t < 0$ . Write  $\sin t$ ,  $\sec t$ , and  $\cot t$  as non-decimal fractions (example  $\frac{1}{2}$  instead of 0.5).

**Solution:** Since  $\tan t < 0$  and  $\cos t < 0$  the terminal side of  $t$  lies in the second quadrant. A point on the terminal side of  $t$  is  $(x, y) = (-12, 5)$ . In this case  $r = \sqrt{(-12)^2 + 5^2} = 13$ . Thus (answers in boldface)

$$\sin t = \frac{y}{r} = \frac{5}{13} \text{ (4 points)}, \quad \cos t = \frac{x}{r} = -\frac{12}{13}, \quad \tan t = \frac{y}{x} = -\frac{5}{12}$$

and by taking reciprocals

$$\csc t = \frac{13}{5}, \quad \sec t = -\frac{13}{12} \text{ (4 points)}, \quad \cot t = -\frac{12}{5} \text{ (4 points)}.$$

2. (8 points) A periodic phenomenon is modeled by  $f(t) = A \sin(bt + c)$ . Suppose that the range of  $f(t)$  is  $[-12, 12]$ , the function  $f(t)$  has period  $3\pi$ , and the phase shift is  $\frac{\pi}{3}$ . Find  $A$ ,  $b$ , and  $c$ .

**Solution:**  $A > 0$  should have been added. Thus  $A = \pm 12$  (2 points) is ok.  $3\pi = \frac{2\pi}{b}$  so  $b = \frac{2}{3}$  (3 points). Since  $\frac{\pi}{3} = -\frac{c}{b}$  it follows that  $c = -\left(\frac{\pi}{3}\right)b = -\frac{2\pi}{9}$  (3 points).