

- ALL WORK MUST BE SHOWN in the booklet for full credit.
- Exact solutions are expected for some problems as instructed, there will be no credit for decimals; NO SHARING OF CALCULATORS.
- Place your exam question sheet INSIDE the booklet when you hand in your exam TO YOUR TA.
- Keep your eyes on your own paper, cheating will be dealt with severely.
- Remember to hand in your special assignment 2.

1. Let $f(x) = \frac{3}{2x+5}$.

- (5 pts) Find the inverse of $f(x)$.
- (5 pts) Show that $f(f^{-1}(x)) = x$.
- (5 pts) State the domain and the range of f .

2. Solve each equation. (Express the solution in an exact form).

(a) (10 pts) $5^{x-2} = 3^{2x+1}$ (b) (10 pts) $\log_2 x^4 - \log_4 x = 7$

3. (a) (7 pts) Find the amount that results from investing \$100 at 6% compounded quarterly after a period of 3 years.

(b) (8 pts) Find the principal (the present value) needed now to get \$300 after 4 years at 8% compounded continuously.

4. A culture of bacteria obeys the law of uninhibited growth.

(a) (5 pts) If N is the number of bacteria in the culture and t is the time in hours, express N as a function of t .

- (b) (10 pts) If 500 bacteria are present initially and there are 800 after 1 hour, how many will be present in the culture after 5 hours? Round your answer to two decimal places.
5. (20 pts) Given $\tan \theta = -\frac{12}{5}$, $\sin \theta > 0$. Find the exact value of each of the remaining trigonometric functions of θ .
6. Given $f(x) = 2 \sin\left(\frac{\pi}{4}x - \pi\right)$.
- (a) (5 pts) Find the amplitude, period, and phase shift of $f(x)$.
- (b) (10 pts) Find the five key points of $f(x)$.