Math 110 Review for Exam 1

1. The picture below displays the graph of a function f.



- a. What is the domain and range of f? Use interval notation.
- b. On which intervals of x is f increasing? Decreasing?
- c. What are the local maximum and minimum values of f, and where do they occur?
- 2. The graph of a function g is displayed below.



Write an explicit rule for g(x), and test it with several values of x.

- 3. Let $g(t) = \begin{cases} 3 t^2 & :t < -1 \\ 2 & :t \ge -1 \end{cases}$, and $h(t) = \begin{cases} 3 & :t \le 0 \\ t & :t > 0 \end{cases}$.
 - a. Sketch the graphs of h and g.
 - b. For what value(s) of t is h(t) = g(t)? For what intervals of t is h(t) > g(t)?
- 4. You are driving on the interstate at a constant speed. You notice you start at mile marker 210. After 1 and a half hours, you notice you pass mile marker 315. Since you are driving at a constant speed (hurray for cruise control), there is a linear relationship between the position you are on the road M (think mile markers) and the time t you have been driving on the interstate since passing that first mile marker you noticed.
 - a. What is the slope between these points, and what is its meaning in this context?

b. Find a linear equation that models the position M (in miles) you are on the road in terms of the time t you have been driving.

c. How long will you have been driving when you reach mile marker 420?

5. The graph of a function f is displayed below.



- a. Using transformations, write down the explicit rule f(x) of the function.
- b. Restrict the domain of f so that it has an inverse f^{-1} , and find a rule for $f^{-1}(x)$.
- c. Use composition to check your answer in from part (b); verify that $f \circ f^{-1}(x) = x$.

6. Let
$$f(x) = \frac{1}{x}$$
, $g(x) = \frac{1}{x^2}$, $h(x) = x - 3$, and $k(x) = \sqrt[3]{7 - 4x}$.

- a. Find f(f(x)) and its domain.
- b. Find f(g(x)) and its domain.
- c. Find g(h(x)) and its domain.
- d. Find $k^{-1}(x)$.
- 7. Observe the following graph of a function f.



Is this function one-to-one? If so, sketch the graph of its inverse on the same coordinate plane. The following problems are from written homework 4.

- 8. Given the quadratic function $f(x) = -x^2 + 8x 7$, answer the following.
 - a. Find the x and y-intercepts for f. Write your answers in point form.
 - b. Find the vertex of f, and write your answer in point form.
 - c. Does f have a minimum or maximum, and what is it?
 - d. Use your answers above to sketch a graph of f.
 - e. What is the domain and range of f?
 - f. On what interval is f increasing, and on what interval is f decreasing?
 - g. On what interval is $f(x) \ge 0$?

9. The number of apples produced by each tree in an apple orchard depends on how densely the trees are planted. If n trees are planted on an acre of land, then each tree produces 900 - 9n apples. So the number of apples produced per acre is

$$A(n) = n(900 - 9n)$$

How many trees should be planted per acre to obtain the maximum yield of apples?

- 10. Given the function $f(x) = 2 + \sqrt{x+3}$, answer the following.
 - a. What is the domain and range of f? Write your answers in interval form.

b. Sketch a graph of f.



- c. Find a formula for $f^{-1}(x)$. Note: Remember, the domain of $f^{-1}(x)$ will match the range of f(x).
- d. Sketch a graph of $f^{-1}(x)$. Just sketch this above on part b's coordinate plane.
- 11. Sketch a graph of the following functions, using transformations of the given functions $f(x) = x^2$, $g(x) = \sqrt{x}$, and h(x) = |x|, respectively. Please state what the transformations are and then graph them.

 $F(x) = -2(x-3)^2 \qquad \qquad G(x) = \sqrt{-\frac{1}{2}x} + 2 \qquad \qquad H(x) = 3 - |x+1|$

12. The discussion sheets from Thursday February 2nd (week 4) and from Tuesday February 7th (week 5) are excellent review as well, so be sure to look over those.