

**Name:** \_\_\_\_\_

**UIN:** \_\_\_\_\_

**T/TH class time:** \_\_\_\_\_

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- You are expected to abide by the University's rules concerning Academic Honesty.
- You may *not* use your books, notes, or any electronic device including calculators and cell phones.
- Show ALL your work. Unsupported answers will not receive credit.
- Always state a complete answer to the problem.

(9 pts) **1.** Suppose that  $h(x) = e^x - 4$ .

a) State the domain of  $h(x)$ .

b) Sketch the graph of  $h(x)$ .

(9 pts) **2.** Suppose that  $g(x) = \log_{1/10}(x^2 + 16) + \log_{1/10}(7 - x)$ . Evaluate  $g$  at  $x = 3$ . Your final answer should not involve logarithms.

(7 pts) **3.** Suppose that  $h(x) = 9^{x-1} - 3$ . If  $h(x) = 24$  find  $x$ . Your final answer should not involve logarithms.

(9 pts) **4.** Suppose that  $f(x) = \ln(x + 5)$ .

a) State the domain of  $f(x)$ .

b) Sketch the graph of  $f(x)$ .

- (12 pts) **5.** Suppose that  $\alpha$  and  $\beta$  are central angles in the unit circle, and  $\alpha = 105^\circ$  while  $\beta = \frac{2}{3}\pi$ .
- a) On the same unit circle draw  $\alpha$  and  $\beta$  in standard position. Indicate the amount and direction of rotation.
  - b) Find the difference between the area of the sector of the unit circle cut by  $\alpha$  and the area of the sector cut by  $\beta$ .

- (15 pts) **6.** Draw each angle in standard position then find the exact value of the trigonometric function:

a)  $\sin\left(-\frac{2\pi}{3}\right)$

b)  $\cos(5\pi)$

c)  $\tan\left(\frac{7\pi}{4}\right)$

- (17 pts) **7.** Suppose that  $\cot \theta = -\frac{3}{4}$  and  $\sin \theta > 0$ . Find the exact value of the remaining trigonometric functions:  $\sin \theta$ ,  $\cos \theta$ ,  $\tan \theta$ ,  $\sec \theta$ ,  $\csc \theta$ .

- (12 pts) **8.** Given a sinusoidal function  $y = -5 \sin(\pi x + \frac{\pi}{3}) + 1$ , find

Amplitude :

Period :

Phase shift :

Vertical shift (centerline) :

- (10 pts) **9.** Sketch the graph of  $y = 2 \sin(x + \pi/6)$ . Include at least two periods and mark key points on your graph.