

Find the exact value of the following.

$$\sin^{-1}\left(\frac{1}{2}\right)$$

$$\tan^{-1}(-1)$$

$$\sec^{-1}(-2)$$

$$\cos^{-1}\left(-\frac{\sqrt{3}}{2}\right)$$

Use Sum/Difference, Double/Half-Angles formulas to find the exact value of the following.

$$\sin 105^\circ$$

$$\tan\left(\frac{7\pi}{12}\right)$$

$$\cos\left(\frac{\pi}{12}\right)$$

$$\sin(22.5^\circ)$$

$$\cos\left(-\frac{\pi}{8}\right)$$

$$\cos\left(\frac{5\pi}{12}\right)\cos\left(\frac{7\pi}{12}\right) - \sin\left(\frac{5\pi}{12}\right)\sin\left(\frac{7\pi}{12}\right)$$

Verify the identity.

$$\frac{\sec x - \cos x}{\sec x} = \sin^2 x$$

$$-\sin x = \sin\left(\frac{\pi}{3} - x\right) - \sin\left(\frac{\pi}{3} + x\right)$$

Solve the following. Leave your answer in the general solution form.

$$\sin(2\theta) = \cos(\theta)$$

$$\tan \beta = 3 \cot \beta$$

If  $\sec x = \frac{3}{2}$  and is in the fourth quadrant, find  $\sin(2x)$ ,  $\cos(2x)$ ,  $\tan(2x)$ .

Sketch a triangle with an acute angle  $\theta$ , and  $\csc \theta = \frac{41}{40}$ . Find the other 5 trigonometric ratios of  $\theta$ .

A 12 ft ladder leans against a building so that the angle between the ground and the ladder is  $72^\circ$ . How high does the ladder reach on the building? Leave your answer exact, and sketch a drawing illustrating the situation.

A 39 ft tree casts a shadow that is 26 ft long. What is the angle of elevation to the sun? Leave your answer exact, and sketch a drawing.