# MATH 180 Exam 1 

October 3, 2017
Directions. Fill in each of the lines below. Then read the directions that follow before beginning the exam. YOU MAY NOT OPEN THE EXAM UNTIL TOLD TO DO SO BY YOUR INSTRUCTOR. This exam contains 8 pages (including this cover page) and 8 problems. After starting the exam, check to see if any pages are missing. Enter all requested information on this page. You are expected to abide by the University's rules concerning Academic Honesty.

## TA Name:

$\qquad$

The following rules apply:

- You may not use your books, notes, calculators, or any electronic device including cell phones. Only pencils/pens allowed.
- You must show all of your work. An answer, right or wrong, without the proper justification will receive little to no credit.
- You must complete your work in the space provided. We will be scanning your answers into our grading system, so any work you do that is out of place, too close to the page border, or on the wrong page will not be graded!


## Circle your instructor.

- Martina Bode
- Jenny Ross
- Drew Shulman
- Matthew Woolf
- Sherwood Hachtman

1. (10 points) Use the limit definition to compute the derivative function $f^{\prime}(x)$ for the function:

$$
f(x)=\sqrt{6 x+1}
$$

2. (12 points) Draw a graph of a function $f(x)$ that satisfies all of the following properties:
(a) $f(4)=15$
(b) $\lim _{x \rightarrow 4} f(x)=10$
(c) $\lim _{x \rightarrow 10^{-}} f(x)=-\infty$
(d) $\lim _{x \rightarrow 10^{+}} f(x)=\infty$
(e) $\lim _{x \rightarrow \infty} f(x)=5$
(f) $\lim _{x \rightarrow-\infty} f(x)=\infty$

3. (24 points) Evaluate the following limits. If the limit is infinite, state whether it is $\infty$ or $-\infty$. Clearly explain your reasoning, stating theorems as needed.
(a) (6 points) $\lim _{z \rightarrow \pi} \frac{2+\cos (z)}{z^{2}+1}$
(b) (6 points) $\lim _{x \rightarrow 3} \frac{x^{2}-10 x+21}{x-3}$
(c) (6 points) $\lim _{x \rightarrow \infty} \frac{3 x^{2}+x+5}{1+5 x+7 x^{2}}$
(d) (6 points) $\lim _{x \rightarrow 2^{-}} \frac{x^{2}}{x-2}$
4. (10 points) A function $f$ is defined by

$$
f(x)= \begin{cases}\cos x & \text { if } x<0 \\ 6 & \text { if } x=0 \\ \sin x+1 & \text { if } x>0\end{cases}
$$

(a) (3 points) Find $\lim _{x \rightarrow 0^{-}} f(x)$.
(b) (3 points) Find $\lim _{x \rightarrow 0^{+}} f(x)$.
(c) (2 points) Find $\lim _{x \rightarrow 0} f(x)$.
(d) (2 points) Is $f$ continuous at $x=0$ ?
5. (10 points) Evaluate $\lim _{x \rightarrow 0} x^{2} \sin (1 / x)$. Clearly explain your reasoning, stating theorems as needed.
6. (20 points) Find the derivatives of the following functions. Do not simplify your answers.
(a) (5 points) $f(t)=9 t-\frac{5}{t^{6}}+3^{4}$
(b) (5 points) $f(x)=\sin \left(7 x^{3}+6 x\right)$
(c) (5 points) $f(x)=\frac{\tan (3 x)}{\sqrt{x}}$
(d) (5 points) Find $h^{\prime}(2)$ given that $h(x)=x^{2}(g(x)+2)$ with $g(2)=3$, and $g^{\prime}(2)=5$.
7. (6 points) The graph of $g(x)$ is shown below.


Sketch the graph of the derivative $g^{\prime}(x)$.

8. (8 points) Fill in the blanks in the left column to complete the statements to show that $x^{3}+2 x=1$ has a solution.
Choose your answers from the items in the column to the right.

Suppose $f(x)=$ $\qquad$
is a continuous function
on the interval $\qquad$

Let $L=$ $\qquad$ be a number
between $\qquad$ and $\qquad$ .

Then by the $\qquad$
there is a $c$ in the interval $\qquad$
such that:

- $f(x)=x^{3}+2 x$
- $f(x)=x^{3}+2 x-1$
- $[0,1]$
- $[1,3]$
- $(0,1)$
- $(1,3)$
- 0
- 1
- 2
- 3
- $f(0)=0$
- $f(0)=-1$
- $f(1)=3$
- $f(1)=2$
- Squeeze Theorem
- Intermediate Value Theorem
- Fundamental Theorem
- $(0,1)$
- $(1,3)$
- $(0,3)$
- $(-1,2)$
- $f(c)=0$
- $f(c)=1$
- $f(c)=2$
- $f(c)=3$

