MATH 210 Exam 1 February 16, 2017

Directions. Fill in each of the lines below. Then read the directions that follow before beginning the exam. YOU MAY NOT OPEN THE EXAM UNTIL TOLD TO DO SO BY YOUR INSTRUCTOR.

Name: _____

UIN: _____

University Email:

Check next to your instructor's name:

| Lukina | |
|-----------|--|
| Abramov | |
| Heard | |
| Woolf | |
| Thulin | |
| Page | |
| Skalit | |
| Kobotis | |
| Freitag | |
| Shulman | |
| Lesieutre | |

- All of your work must fit within the boxes on each page for each question. Nothing outside of the box will be graded! If you write outside of the box, there is a good chance that your solution will not be read and therefore not graded.
- A solution for one problem may not go on another page.
- Show all your work. Unjustified answers are not correct. Make clear what your final answer is.
- Have your student ID ready to be checked when submitting your exam.

1. (10 pt) Let $\mathbf{u} = \langle 1, 2, 1 \rangle$ and $\mathbf{v} = \langle -2, 1, 2 \rangle$

- (a) Compute $3\mathbf{u} 2\mathbf{v}$.
- (b) Compute $\mathbf{u} \cdot \mathbf{v}$.
- (c) Determine if \mathbf{u} and \mathbf{v} are parallel, orthogonal, or neither. Justify your answer.

- 2. (15pt) Consider the points P(1, 2, 3), Q(4, 5, 6), R(0, 2, 0).
 - (a) Compute the vectors A and A

- 3. (15pt) Write down the equations for the following lines:
 - (a) The line through the point (0, 1, 1) parallel to the line $\mathbf{r}(t) = \langle 2t, 3 4t, -1 + 7t \rangle$.
 - (b) The line through the point (2, 1, 2) perpendicular to the plane x 3y + z = 1.

4. (15 pt) A particle moves in space with acceleration given by the vector-valued function

 $\mathbf{a}(t) = \langle t, 2t, \cos t \rangle.$

Time t is measured in seconds. At time t = 0 the particle is located at the origin (0, 0, 0) and has the velocity $\mathbf{v}_0 = \langle 0, 1, 0 \rangle$.

(a) Compute the velocity function $\mathbf{v}(t)$.

(b) Compute the position function $\mathbf{r}(t)$.

5. (10 pt) Let $z = f(x, y) = 2\sqrt{9 - x^2 - y^2}$.

- (a) State the domain of f. Give a rough sketch of this region in the xy plane; be sure to shade in the area belonging to the domain.
- (b) Find the equations of level curves for $z = 2\sqrt{5}$ and for $z = 2\sqrt{8}$. Sketch the level curves on the same picture as the domain of f.

- 6. (10 pt) Let $\mathbf{r}(t) = \langle t^3 9t, t^2 e^t, 6t^2 \rangle$.
 - (a) Compute $\frac{d\mathbf{r}}{dt}$.
 - (b) Compute the tangent vector for t = -1.
 - (c) Compute the equation of the line $\ell(t)$ tangent to the graph of $\mathbf{r}(t)$ for t = -1.

7. (10 pt) Find all four second order partial derivatives of the function

 $f(x,y) = 3xe^y - x^2y + 5.$

- 8. (15 pt) Consider the function $f(x, y) = 3x^2 + 4y^2 2$.
 - (a) Compute the gradient $\nabla f(x, y)$.
 - (b) Find the directional derivative of f(x, y) at the point (1, 1) in the direction of the vector $\mathbf{u} = \langle \frac{1}{2}, \frac{\sqrt{3}}{2} \rangle$.
 - (c) Find the unit vector in the direction of maximum increase and the rate of maximum increase at (1, 1).