Algebraic Geometry Seminar

Two stabilizations in algebraic geometry: Hurwitz spaces and Bott periodicity

Ravi Vakil (Stanford University)

Abstract: A recurring theme in geometry and topology is that moduli spaces become better and better behaved "in the limit".

- (i) Stabilization of the Grothendieck ring is one algebro-geometric analogue of stabilization in topology. After briefly introducing stabilization in the Grothendieck ring (joint with Wood), I will describe how it applies to low-degree Hurwitz spaces (in analogy with Bhargavology), which is made simpler thanks to powerful ideas of Bilu and Howe. (This is joint with Landesman and Wood.)
- (ii) H. Larson recently completely described (integrally) the "characteristic classes" of vector bundles on P^1 -bundles, in the Chow ring. Bott periodicity relates vector bundles on a topological space X to vector bundles on $X \times S^2$: the "moduli space" BU of complex vector bundles is "basically the same as" the "moduli space" maps of a sphere to BU. I will try to explain an algebro-geometric incarnation of Bott periodicity. (This is work in progress with H. Larson.)