Abstract: Let $C$ be a curve of genus $g$. A fundamental problem in the theory of algebraic curves is to understand maps of $C$ to projective space of dimension $r$ of degree $d$. When the curve $C$ is general, the moduli space of such maps is well-understood by the main theorems of Brill–Noether theory. However, in nature, curves $C$ are often encountered already equipped with a map to some projective space, which may force them to be special in moduli. The simplest case is when $C$ is general among curves of fixed gonality. Despite much study over the past three decades, a similarly complete picture has proved elusive in this case. In this talk, I will discuss joint work with Eric Larson and Isabel Vogt that completes such a picture, by proving analogs of all of the main theorems of Brill–Noether theory in this setting.