MTHT 530 Analysis for Teachers II Problem Set 11

Due: Wednesday April 19

1) Decide if the following series coverges or diverges. Justify your answers and state explicitly which test or tests you are using.

a)
$$\sum_{n=1}^{\infty} \frac{n^2}{3^n}$$

b)
$$\sum_{n=2}^{\infty} \frac{1}{(\ln(n))^2}$$

c)
$$\sum_{n=2}^{\infty} \frac{1}{n \ln n}$$

d)
$$\sum_{n=2}^{\infty} \frac{1}{n(\ln n)^2}$$

e)
$$\sum_{n=1}^{\infty} \frac{n^5}{2^n + n^2}$$

2) a) Show that if $a_n > 0$ for all n and $\lim na_n = L \neq 0$, then $\sum a_n$ diverges.

- b) Assume $a_n > 0$ and $\lim n^2 a_n$ exists. Show that $\sum a_n$ converges.
- 3) Suppose $\sum a_n$ and $\sum b_n$ converge. Show that

$$\sum_{n=1}^{\infty} (a_n + b_n) = \sum_{n=1}^{\infty} a_n + \sum_{n=1}^{\infty} b_n.$$